

Correlation structure of STAR events

CINPP, Kolkata, India.

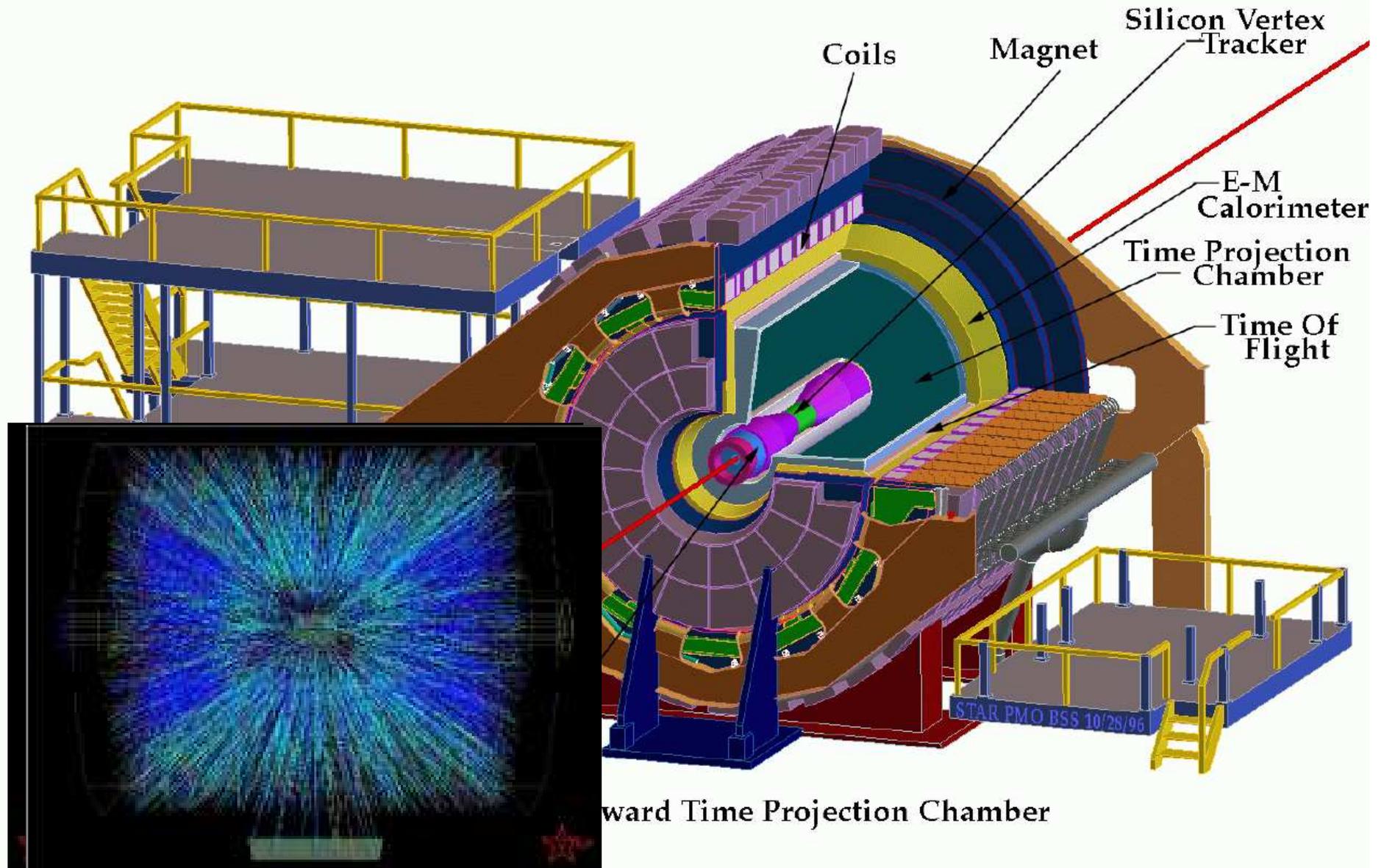
Mikhail Kopytine for the STAR Collaboration

Kent State University

<http://www.star.bnl.gov/~kopytin/>

February 4, 2005

STAR Detector



1 Content of the talk

- Equilibration

Arguably the central issue of RHIC hadronic physics. Is it taking place ? What is the mechanism ? And **what** is equilibrating ?

- Methods

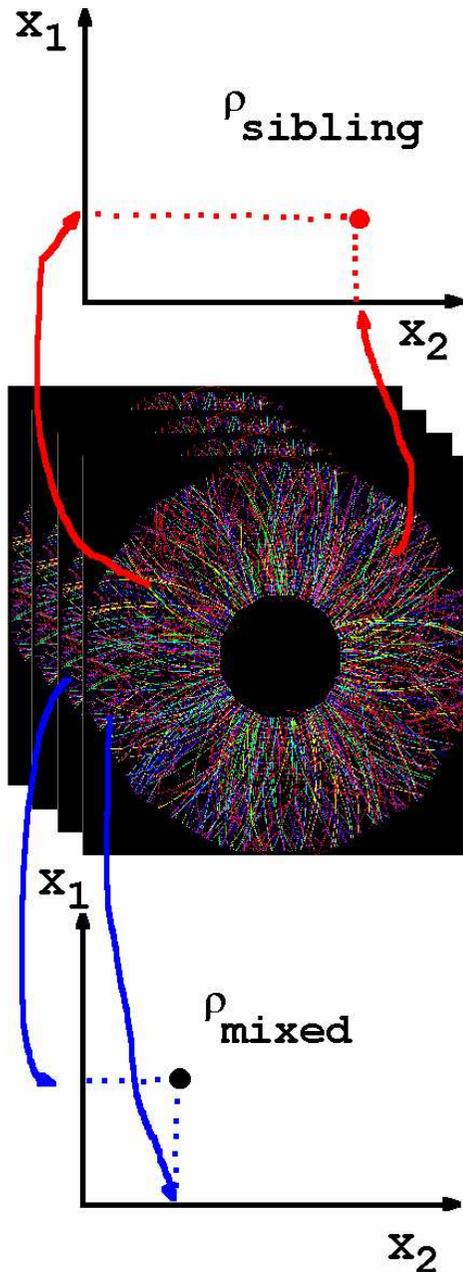
Initial state: a “calibrated” source of correlations. Watch their evolution into final state in time = system size.

- Direct construction of a correlation function.
- Inversion of scale-dependent variance
- Discrete Wavelet Transform

- Observations

- Conclusions

2 Autocorrelation

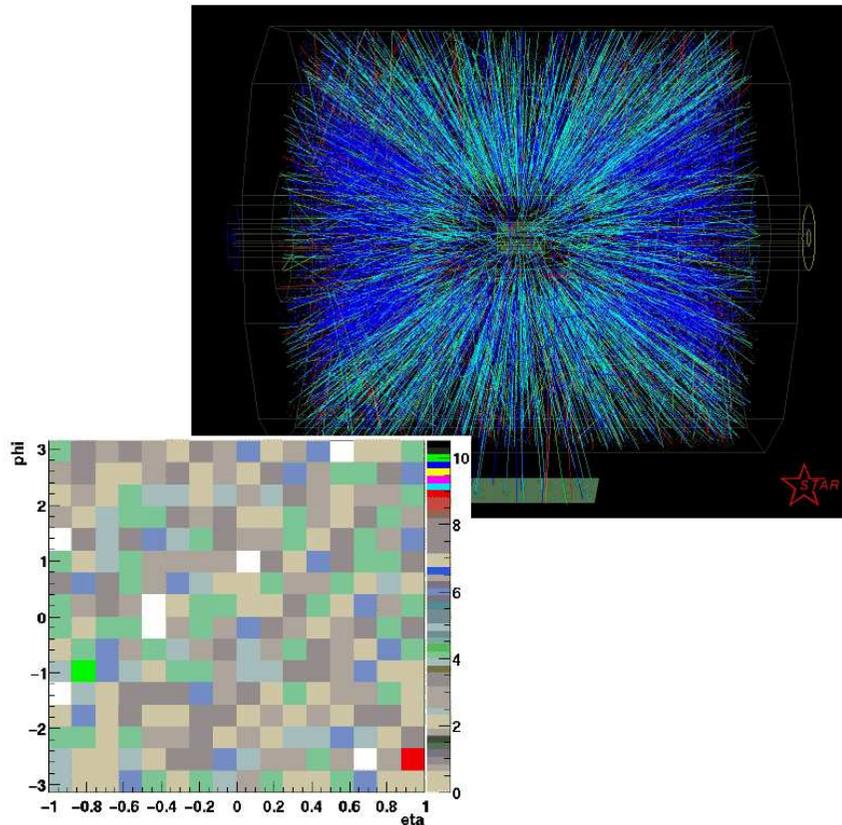


$$\begin{pmatrix} x_1 \\ x_2 \end{pmatrix} \rightarrow \begin{pmatrix} x_{\Sigma} \equiv x_1 + x_2 \\ x_{\Delta} \equiv x_1 - x_2 \end{pmatrix},$$

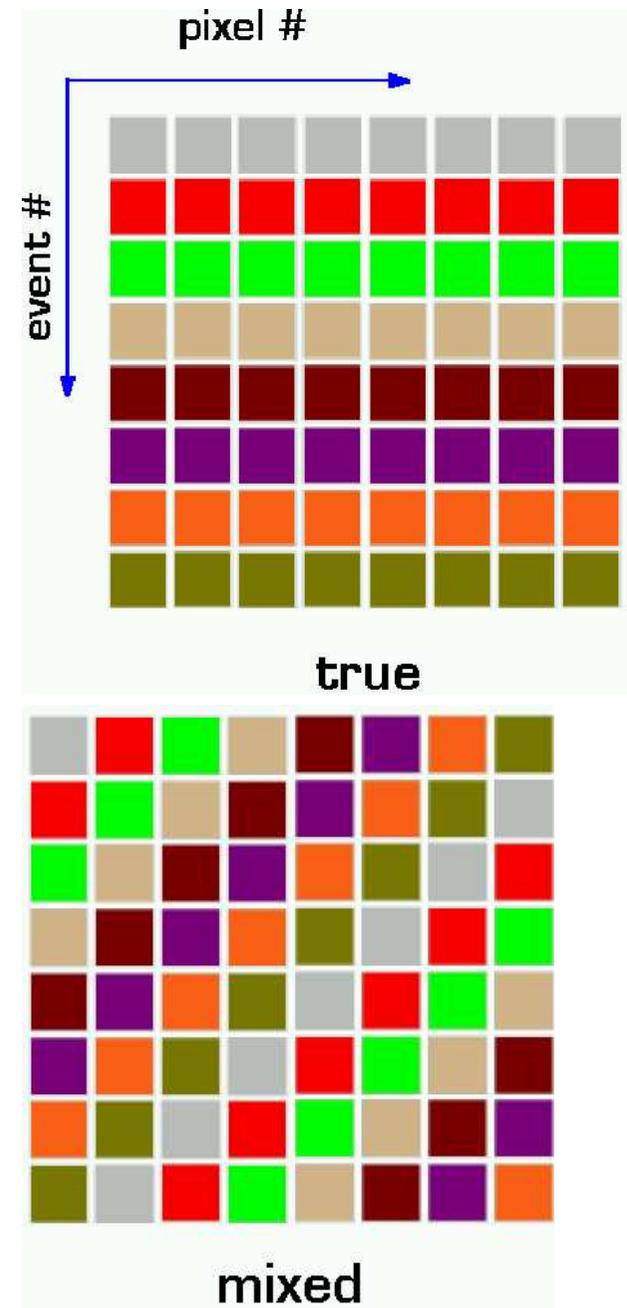
always a lossless transformation of data. **Autocorrelation** A is a projection of a two-point distribution onto difference variable(s) x_{Δ} , lossless for x_{Σ} -invariant (homogenous, stationary) problems.

$$\Delta R(x_1, x_2) = \frac{\rho(x_1, x_2)}{\rho_{\text{ref}}(x_1, x_2)} - 1$$

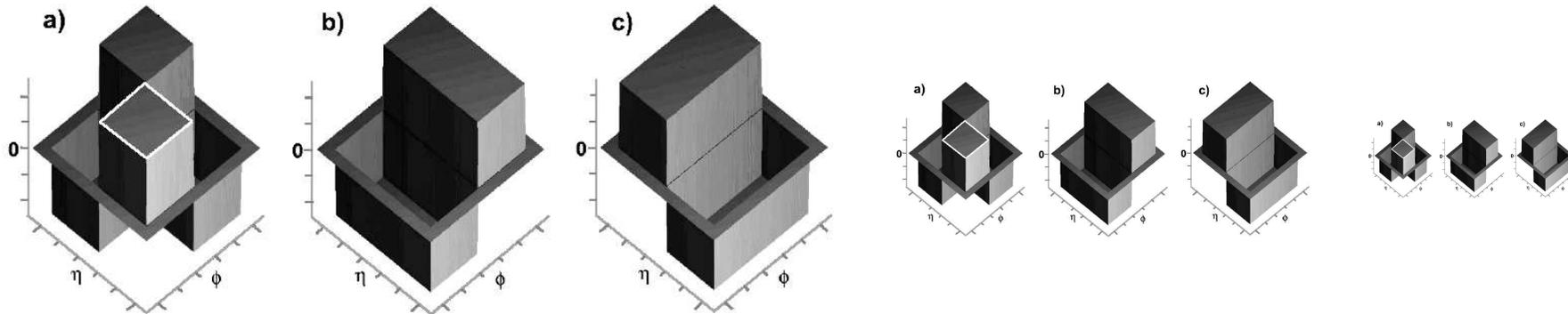
3 Uncorrelated event reference for DWT



mixed events: no pixel used twice; ≤ 1 pixel from any event in the same mixed event; no mixing of events with largely different multiplicity and vertex.



4 Local hadron density fluctuations and Discrete Wavelet Transform (DWT)



$F_{m,l,k}^\lambda(\phi, \eta)$ —Haar wavelet **orthonormal basis** in (ϕ, η) . scale fineness (m), directional modes of sensitivity (λ), track density $\rho(\eta, \phi, p_t)$, locations in 2D (l, k). **DWT is an expansion in this basis.**

Power of local fluctuations, mode λ :

$$P^\lambda(m) = 2^{-2m} \sum_{l,k} \langle \rho, F_{m,l,k}^\lambda \rangle^2 \quad (1)$$

“dynamic texture”:

$$P_{\text{dyn}}^\lambda(m) \equiv P_{\text{true}}^\lambda(m) - P_{\text{mix}}^\lambda(m) \quad (2)$$

Normalized:

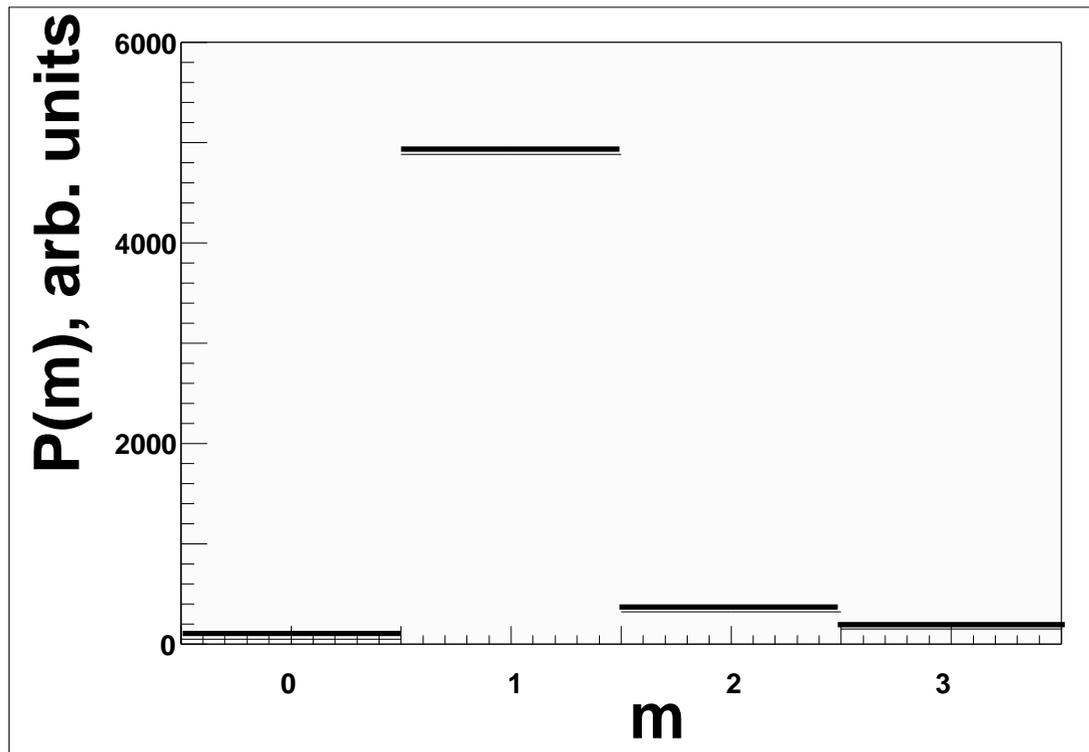
$$P_{\text{dyn}}^\lambda(m) / P_{\text{mix}}^\lambda(m) / n(p_t) \quad (3)$$

5 A flow-like example



Elliptic flow-inspired example:
 x axis – an angle in “natural units” ($2\pi = 1$), y axis – multiplicity. The multiresolution theorem: $a_4 = a_0 + b_0 + b_1 + b_2 + b_3$, can have better fineness.

6 Example of a DWT power spectrum

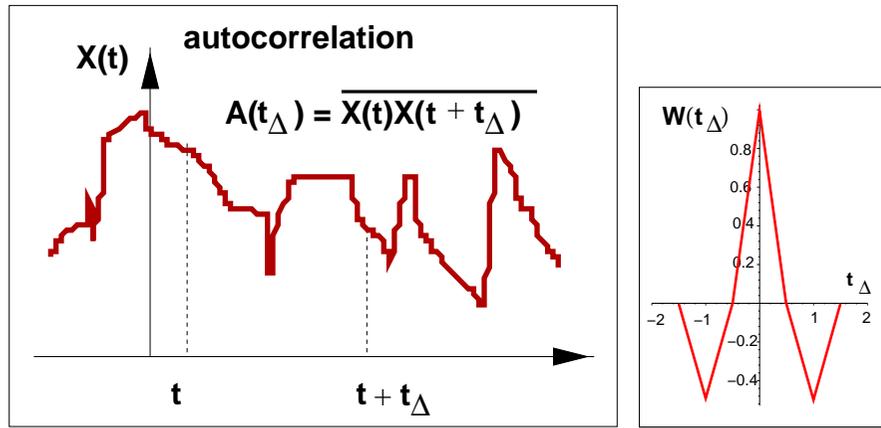


Power spectrum of that flow event as a function of “fineness” m . The dominant contribution is $m = 1$ (the “ v_2 ” harmonic, **b1**). Statistical fluctuations also contribute.

$$P(m) = 2^{-m} \sum_i \langle \rho, F_{m,i} \rangle^2.$$

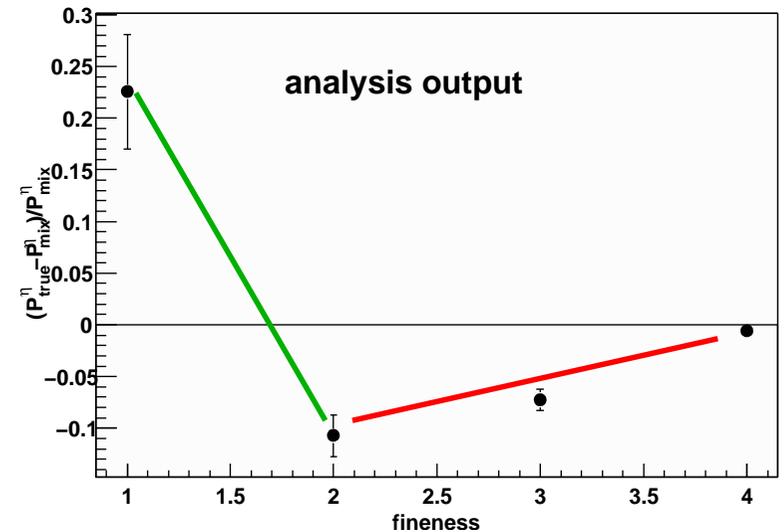
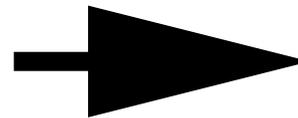
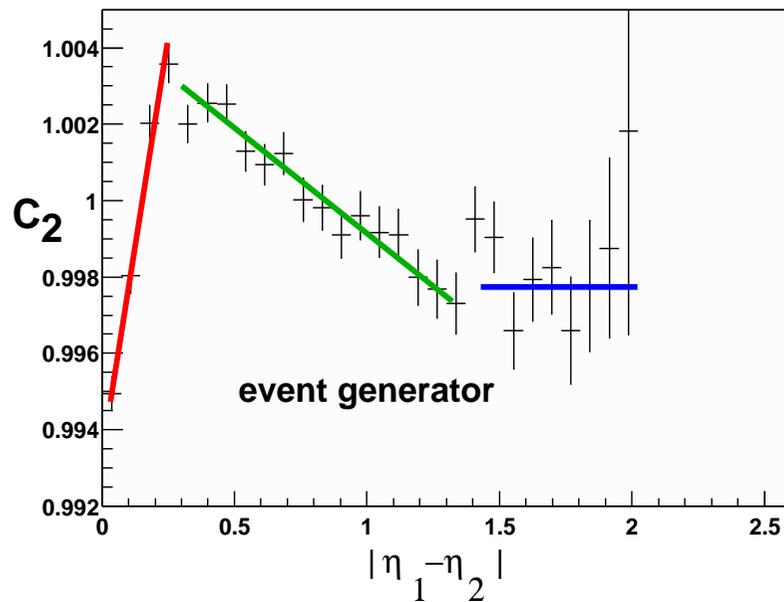
Computational complexity $O(N)$!

7 “Dynamic texture” as a nonparametric measure of the correlation shape

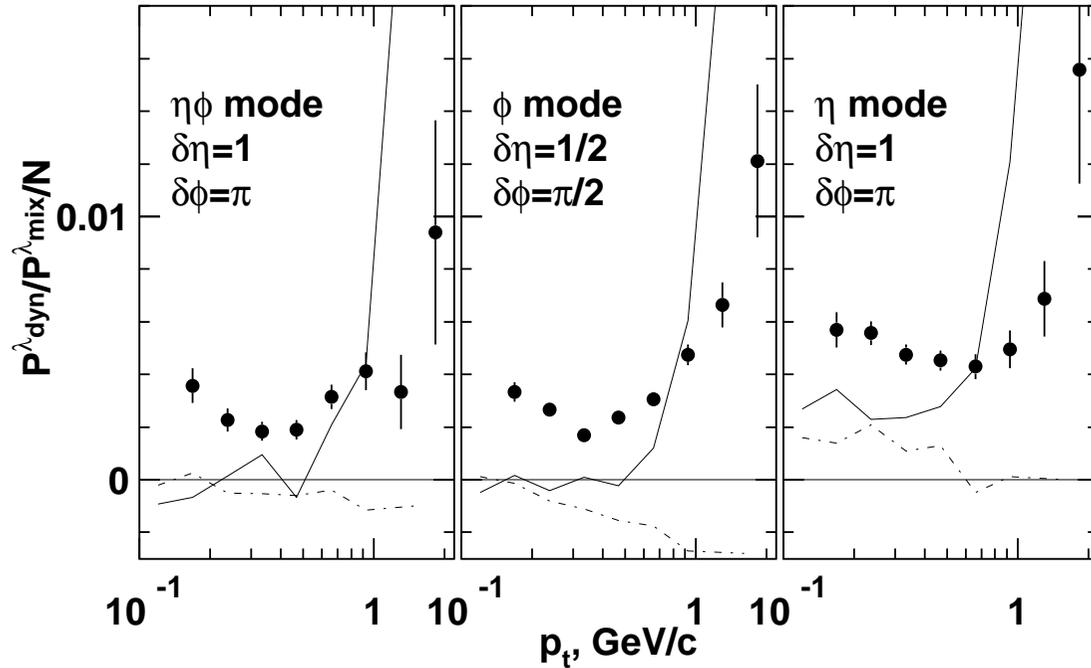


$$P(m) = \overline{\int_{-\infty}^{\infty} X(\tau/2)X(-\tau/2)W(\tau, m) d\tau},$$

where W is the weight function for the Haar wavelet. $P(m)$ reflects differential structure on scale m . See example:



8 “Dynamic texture” p_t dependence: peripheral events, $\sqrt{s_{NN}} = 200$ GeV

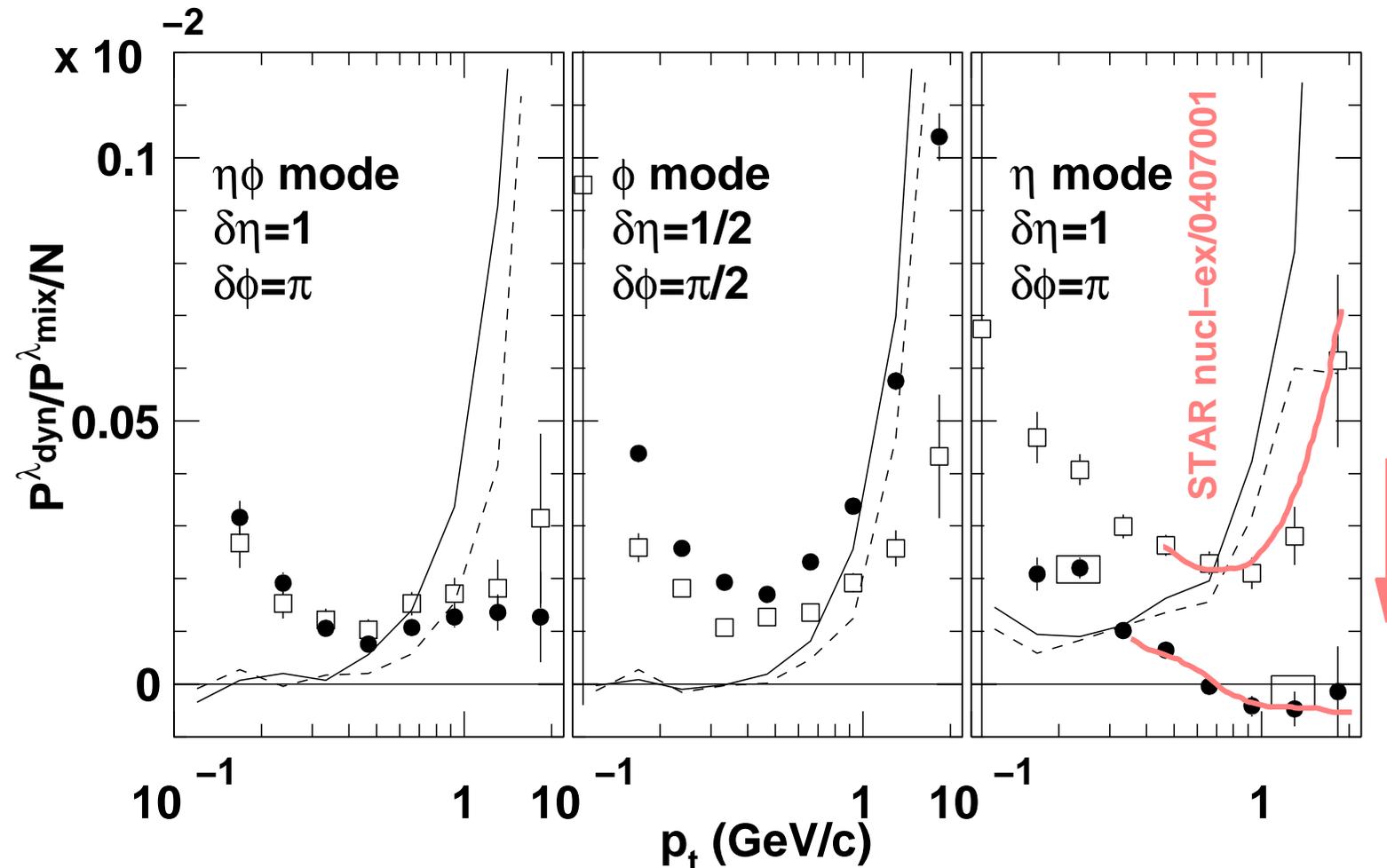


Peripheral (60-84%) events: normalized dynamic texture for fineness scales $m = 0, 1, 0$ from left to right panels, respectively, as a function of p_t . ● – STAR data; solid line – standard HIJING, dash-dotted line – HIJING without jets.

Qualitative trends in peripheral data are as expected. What signal to expect in the central data, if correlation does not change ?

$$\left(\frac{P_{\text{true}}}{P_{\text{mix}}} - 1 \right) \frac{1}{N} \Big|_{\text{centr}} = \left(\frac{P_{\text{true}}}{P_{\text{mix}}} - 1 \right) \Big|_{\text{periph}} \frac{1}{N_{\text{centr}}} \quad (4)$$

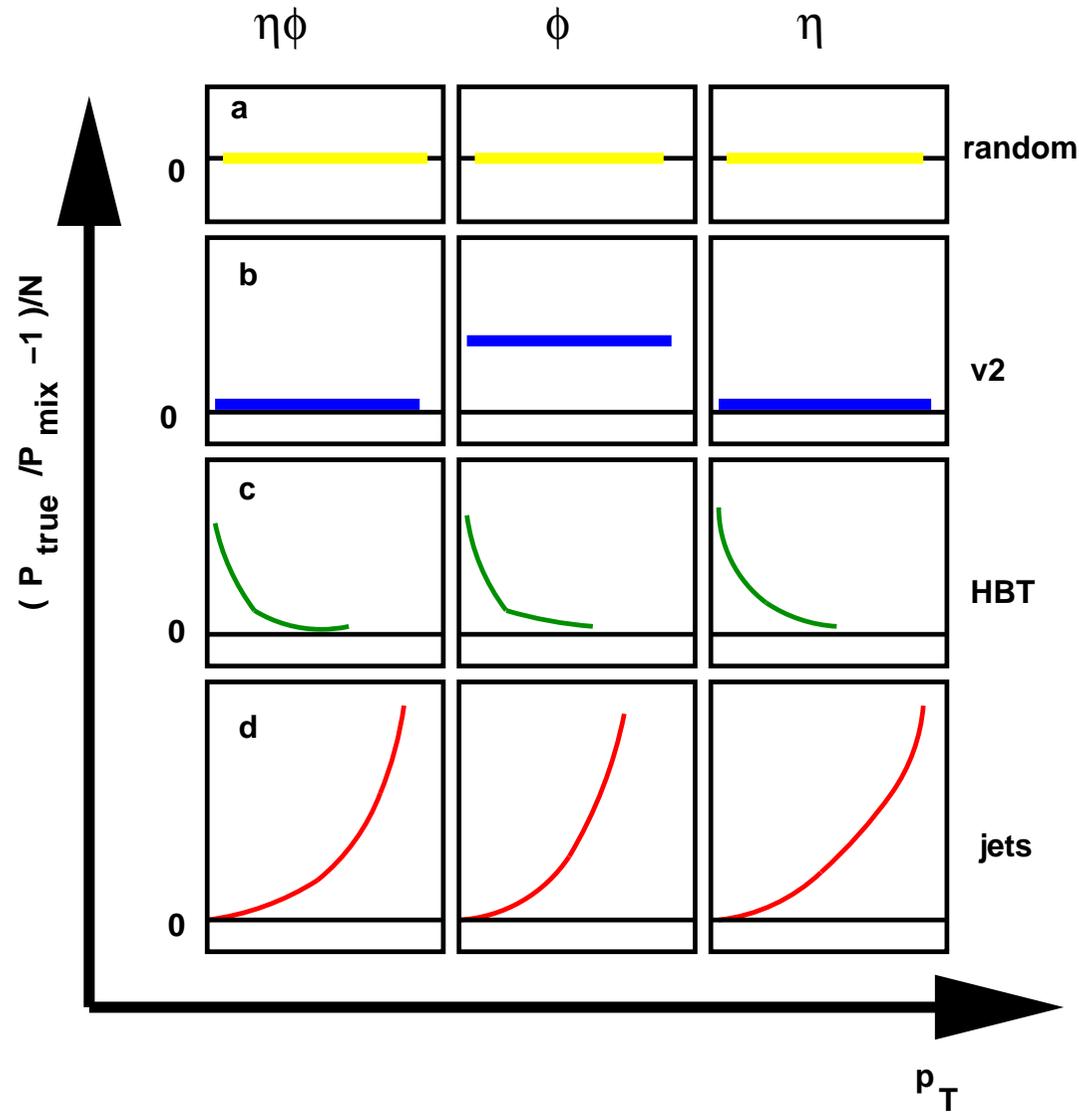
9 Longitudinal minijet broadening: DWT data



Central (top 4%) events: normalized dynamic texture for fineness scales $m = 0, 1, 0$ from left to right panels, respectively, as a function of p_t .

● STAR data; solid line – Hijing without jet quenching; dashed line – Hijing with quenching; □ peripheral STAR data renormalized to compare.
 Minijet elongation \Rightarrow correlation broadening \Leftrightarrow reduced correlation gradient \Leftrightarrow reduced “texture”

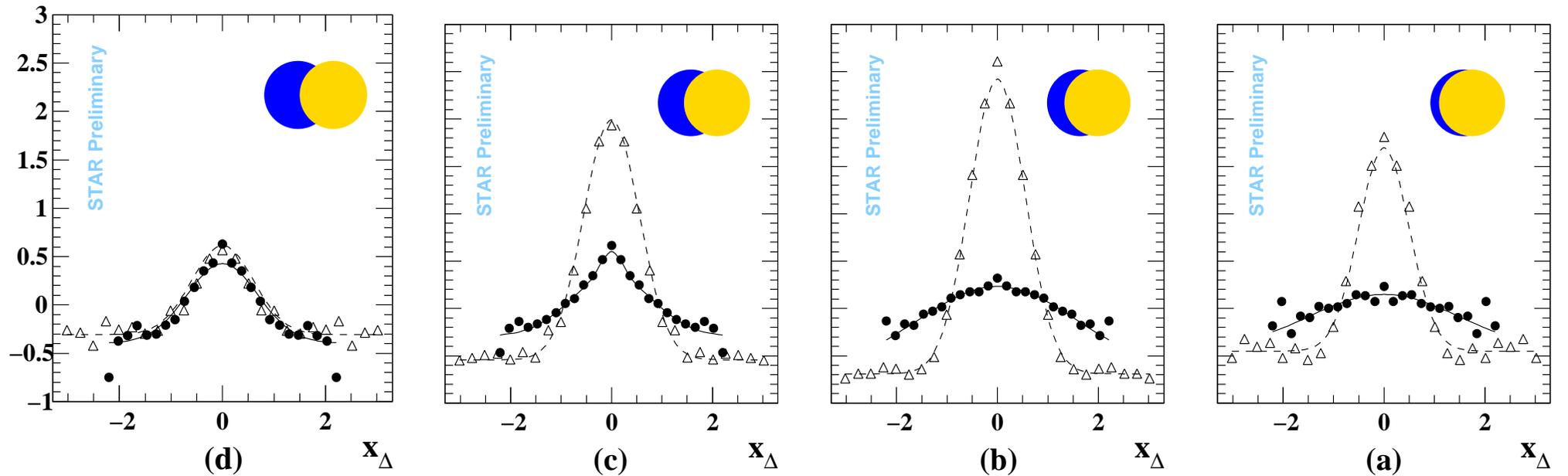
10 “Dynamic texture” response



Dynamic texture response in various idealized situations (showing only one scale):

- (a) events of random (uncorrelated) particles
- (b) p_t -independent elliptic flow
- (c) Correlations at low Q_{inv} (Bose-Einstein correlations and Coulomb effect)
- (d) HIJING jets

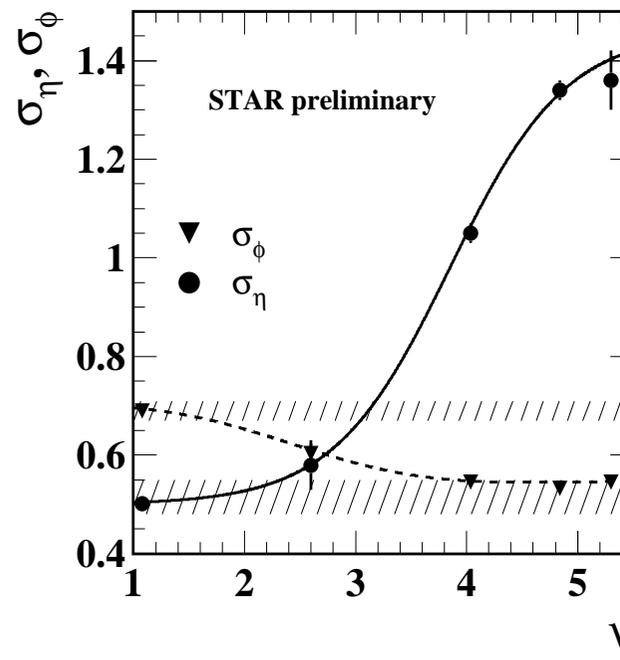
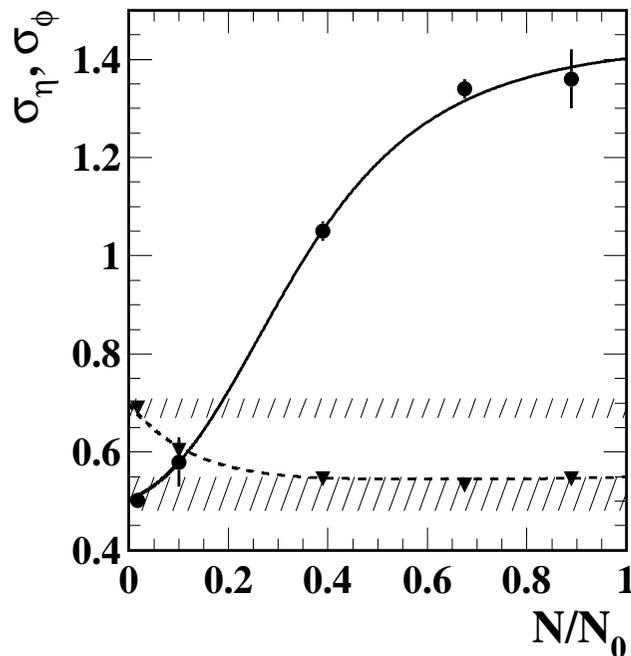
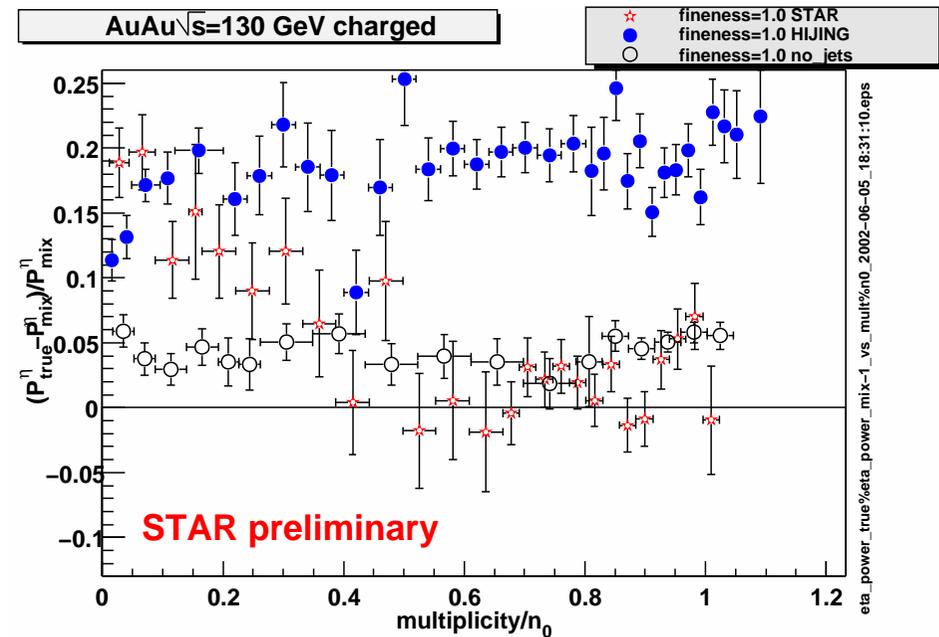
11 Longitudinal minijet broadening: correlation data



Projections of $\bar{N}[\rho(\eta_\Delta, \phi_\Delta)/\rho(\eta_\Delta, \phi_\Delta)_{\text{ref}} - 1]|_{CI}$ on x_Δ which is ϕ_Δ (Δ) or η_Δ (\bullet). v_1 and v_2 are subtracted.

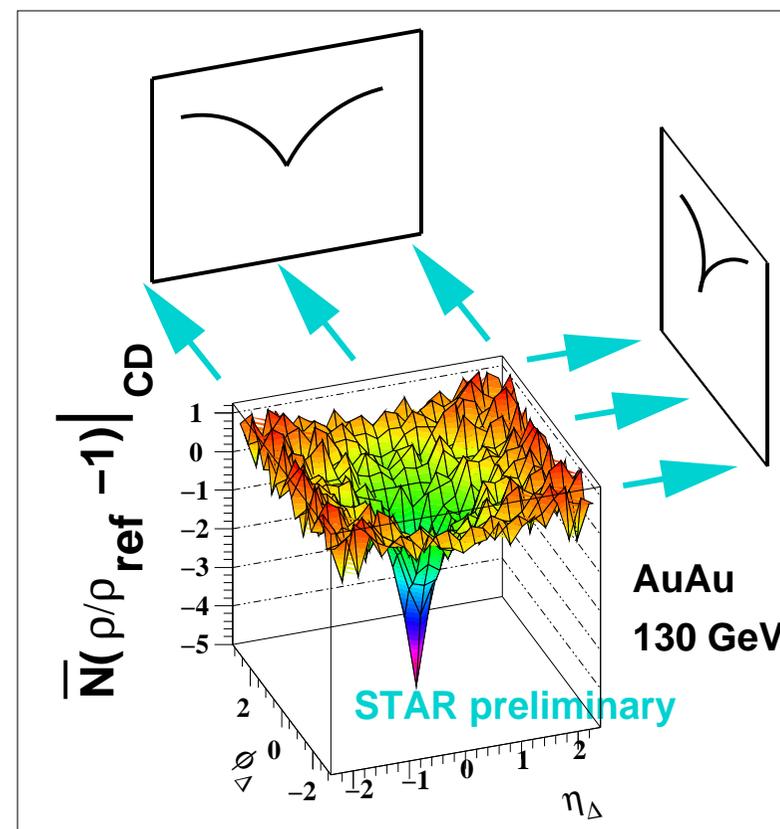
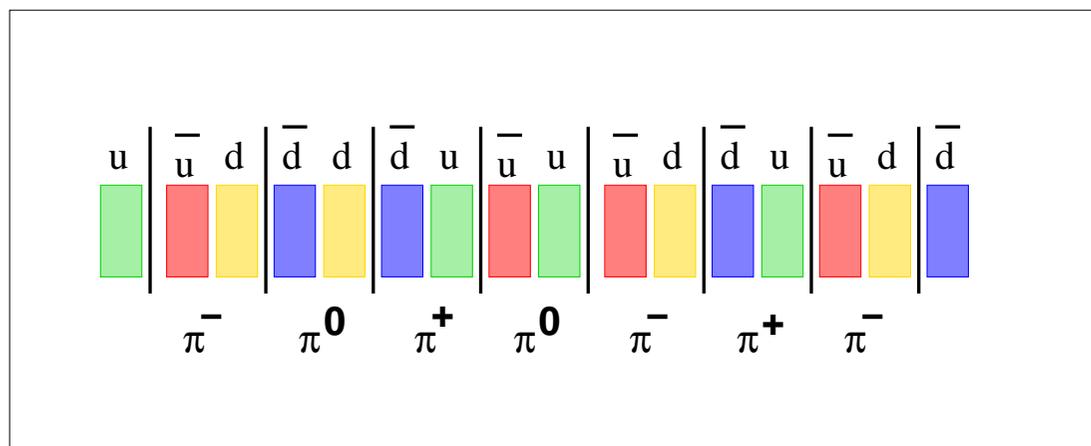
12 Longitudinal minijet broadening: centrality dependence

nucl-ex/0211015. STAR DWT analysis of charge-independent correlations, AuAu, $\sqrt{s_{NN}} = 130$ GeV



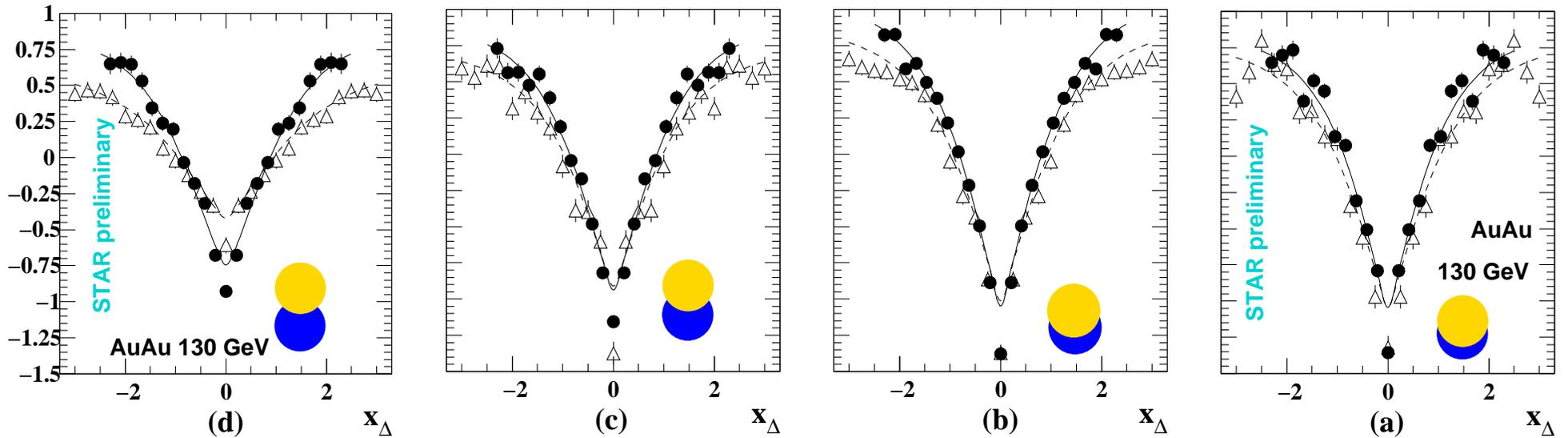
nucl-ex/0411003. STAR two-particle correlation analysis. The step-like character of the centrality dependence is elucidated using

13 Charge-dependent correlations = Like sign - Unlike sign

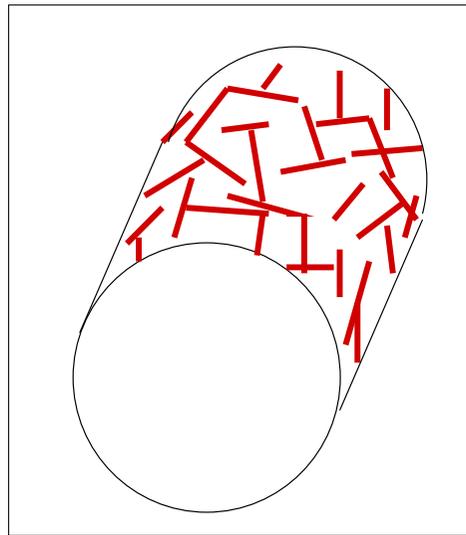
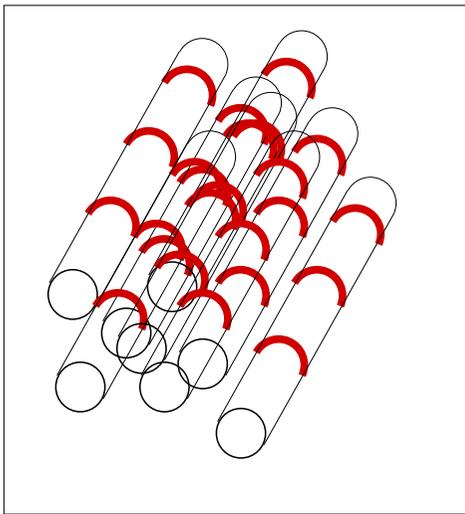


The driving physics: charge conservation in hadronization. Suppress short range correlations – BEC and conversion e^+e^- – by a kinematic pair cut. The \bar{N}_x is good when number of correlation sources $\propto N$.

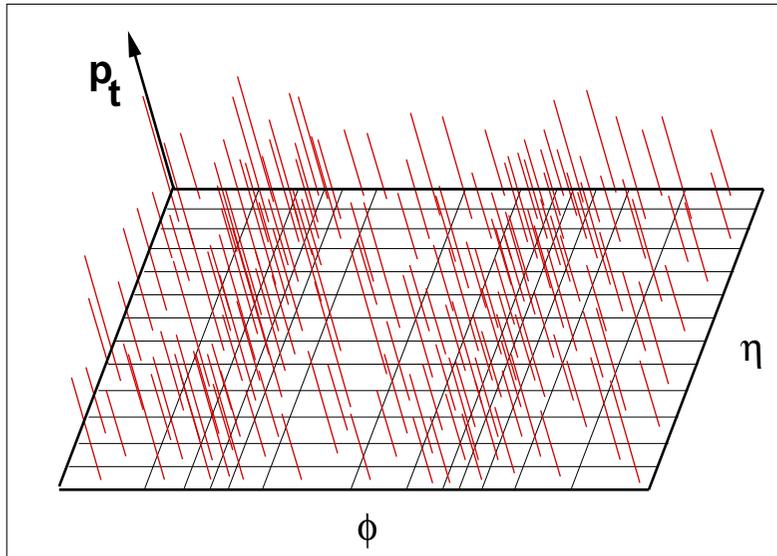
14 Modified hadronization geometry ?



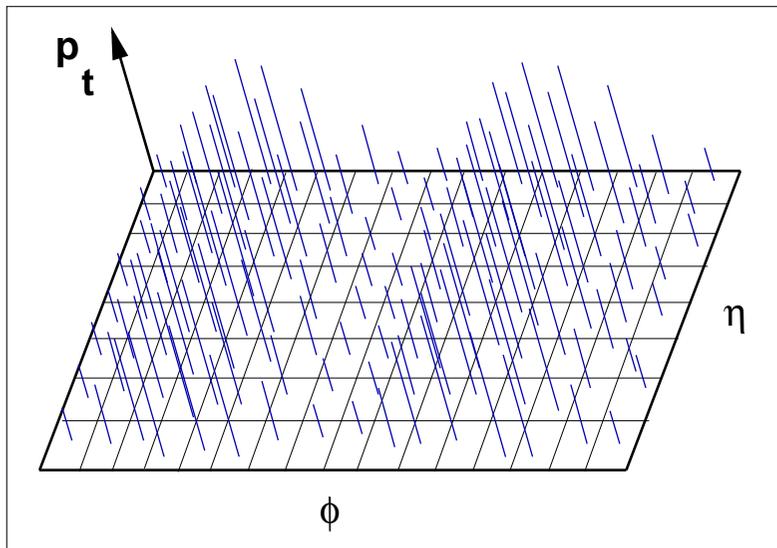
Projections of $\bar{N}(\rho(\eta_\Delta, \phi_\Delta)/\rho(\eta_\Delta, \phi_\Delta)_{\text{ref}} - 1)|_{CD}$ on x_Δ which is ϕ_Δ (Δ) or η_Δ (\bullet). $\eta - \phi$ width disparity (d, peripheral) is gone in (a) \Rightarrow transition from (string) 1D to bulk ($>2D$) fragmentation symmetrizes η and ϕ .



15 Number and p_t correlations



This p_t field may have elliptic flow (number effect). Abounds at RHIC.



Also elliptic... flow (p_t effect) !
Pro: blast wave fits. Is there a **direct** measurement ?

16 Towards p_t correlation/fluctuation analysis

Problem: need to tell apart $p_{t,i}$ and number contributions to the

$p_t \equiv \sum_{i \in (\eta, \phi) \text{ bin}} p_{t,i} \Rightarrow$ can extract the p_t correlation alone.

Solution: use $p_t - n\hat{p}_t$

Q: When is the n -contribution into $\text{Var}[p_t - n\hat{p}_t]$ canceled ?

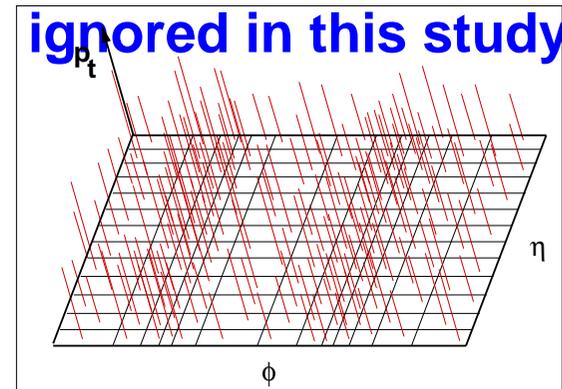
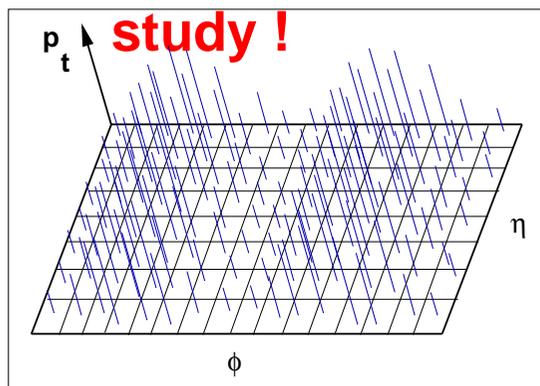
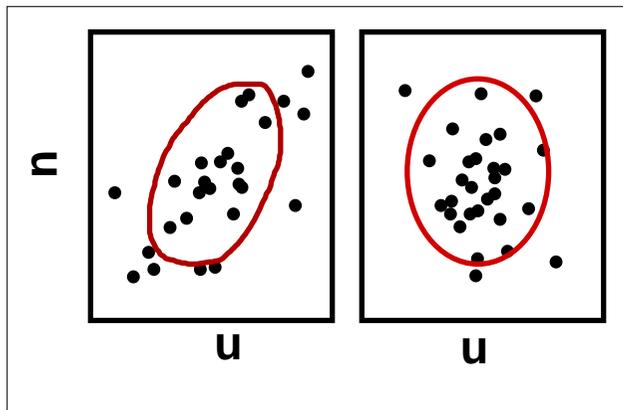
$$\sigma^2(p_t : n) \equiv \text{Var}[p_t - n\hat{p}_t] = \text{Var}[p_t] + \hat{p}_t^2 \text{Var}[n] - 2\hat{p}_t \text{Cov}[n, p_t] \quad (5)$$

$$\text{Var}[p_t] = \text{Var}\left[\sum_i^n p_{t,i}\right] = \text{Var}\left[\sum_i^n (\hat{p}_t + u_i)\right] = \hat{p}_t^2 \text{Var}[n] + \text{Var}[u] + 2\hat{p}_t \text{Cov}[n, u] \quad (6)$$

$$\text{Cov}[n, p_t] = \overline{np_t} - \bar{n}\bar{p}_t = \hat{p}_t \text{Var}[n] \quad (7)$$

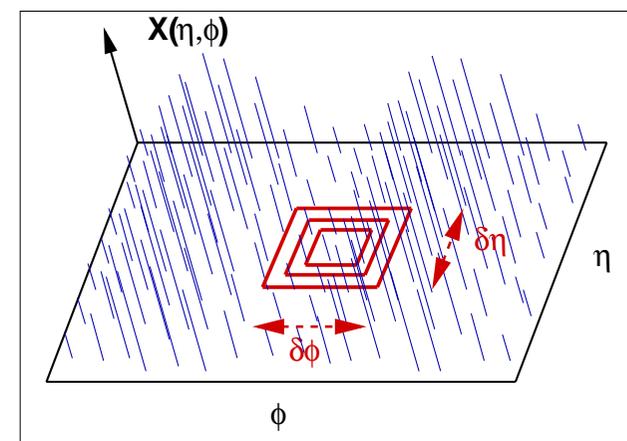
A: For independent p_t and n production, when $\text{Cov}[n, u] \equiv \overline{nu} = 0$, where

$u \equiv \sum_i^n u_i$, $u_i = p_{t,i} - \hat{p}_t$.



17 Get correlations from fluctuations

Extract correlation structure of random field X from the scale dependence of variance (van Marcke "Random Fields" MIT 1983; Trainor, Porter, Prindle hep-ph/0410180)



$$\text{Var}[X; \delta\eta, \delta\phi] = \int_{-\delta\eta/2}^{\delta\eta/2} d\eta_1 \int_{-\delta\phi/2}^{\delta\phi/2} d\phi_1 \int_{-\delta\eta/2}^{\delta\eta/2} d\eta_2 \int_{-\delta\phi/2}^{\delta\phi/2} d\phi_2 \quad (8)$$

$$\times [\overline{X(\eta_1, \phi_1)X(\eta_2, \phi_2)} - \overline{X(\eta_1, \phi_1)} \times \overline{X(\eta_2, \phi_2)}]$$

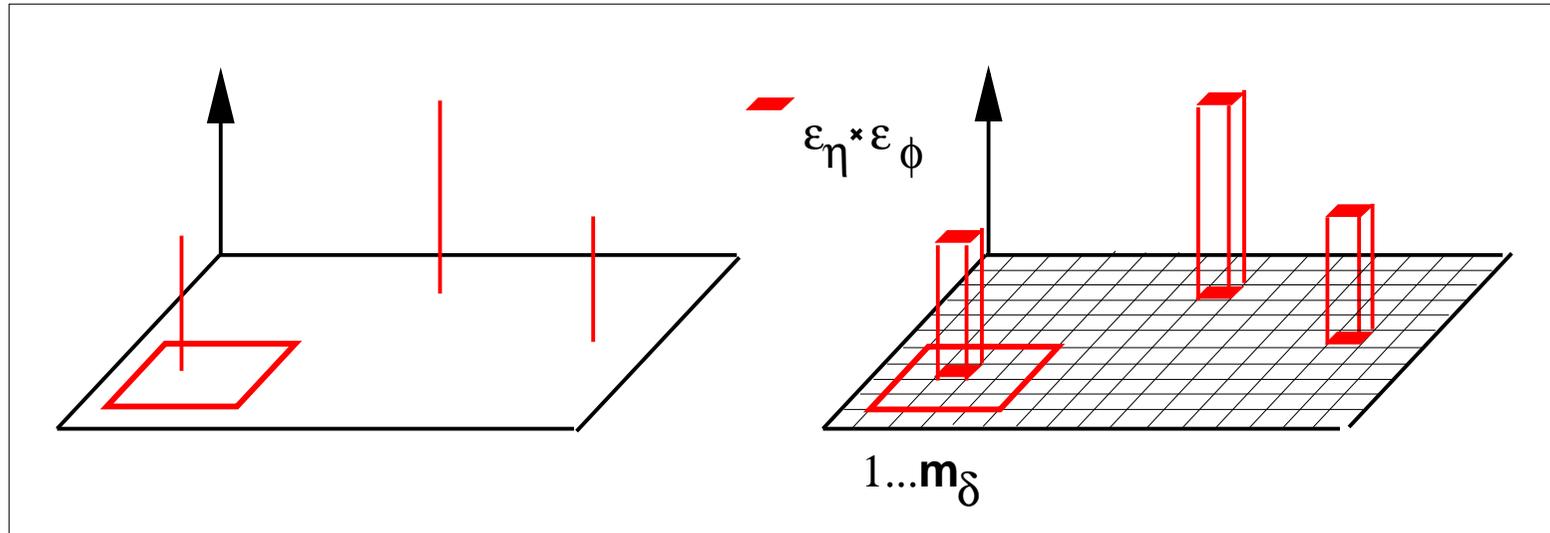
Compare with uncorrelated reference; recognize autocorrelation $\rho(X, t_\Delta) \equiv \overline{X(t)X(t + t_\Delta)}$ (t -average).

$$\Delta\sigma^2(X, \delta\eta, \delta\phi) = \quad (9)$$

$$\int_{-\delta\eta/2}^{\delta\eta/2} d\eta_1 \int_{-\delta\phi/2}^{\delta\phi/2} d\phi_1 \int_{-\delta\eta/2}^{\delta\eta/2} d\eta_2 \int_{-\delta\phi/2}^{\delta\phi/2} d\phi_2 \Delta\rho(X, \eta_1 - \eta_2, \phi_1 - \phi_2) \quad (10)$$

$$= 2 \int_0^{\delta\eta} d\eta_\Delta 2 \int_0^{\delta\phi} d\phi_\Delta (\delta\eta - \eta_\Delta)(\delta\phi - \phi_\Delta) \Delta\rho(X, \eta_\Delta, \phi_\Delta) \quad (11)$$

18 The actual analysis is discrete: $\int \rightarrow \Sigma$



kernel K :

$$(\delta\eta - \eta_\Delta)(\delta\phi - \phi_\Delta) \rightarrow \varepsilon_\eta \varepsilon_\phi K_{m_\delta n_\delta:kl} \equiv \varepsilon_\eta \varepsilon_\phi (m_\delta - k + \frac{1}{2})(n_\delta - l + \frac{1}{2}) \quad (12)$$

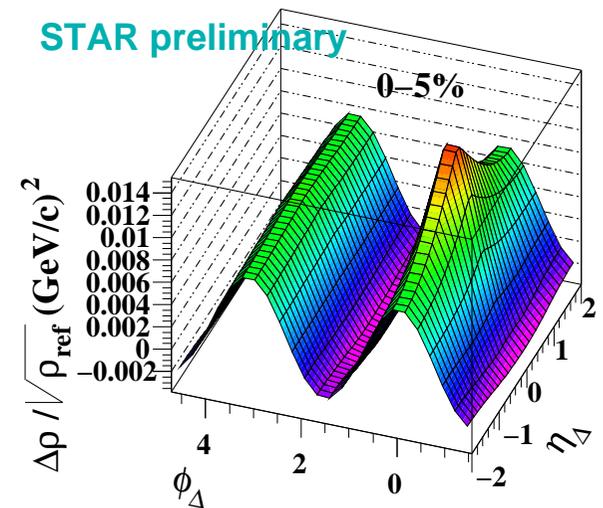
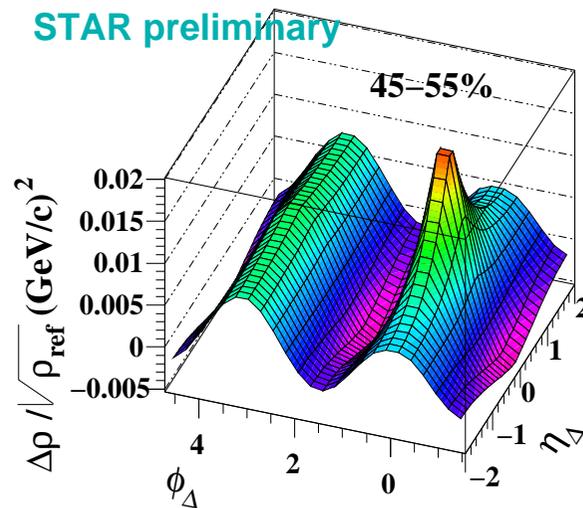
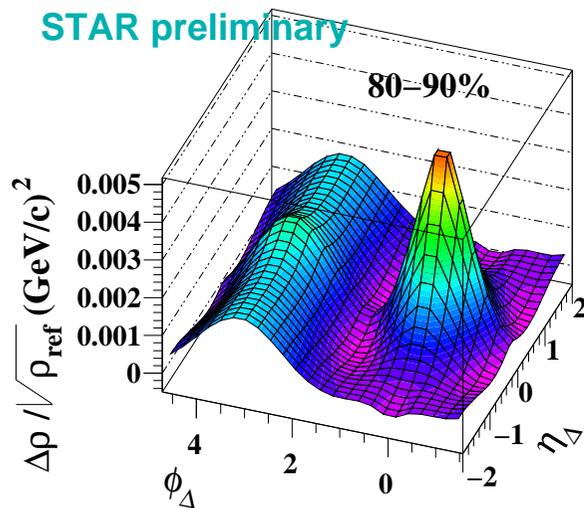
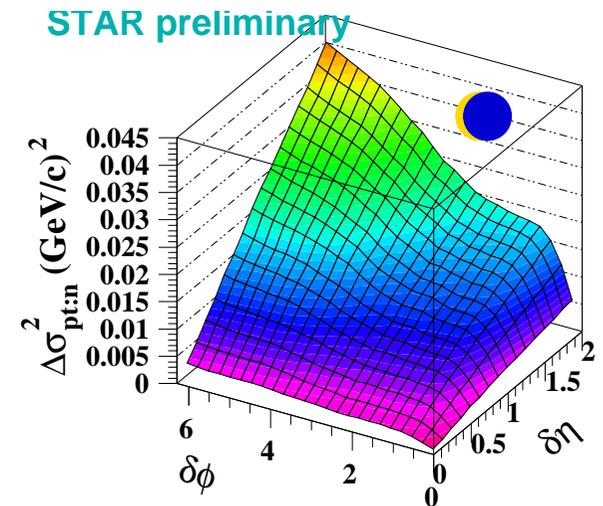
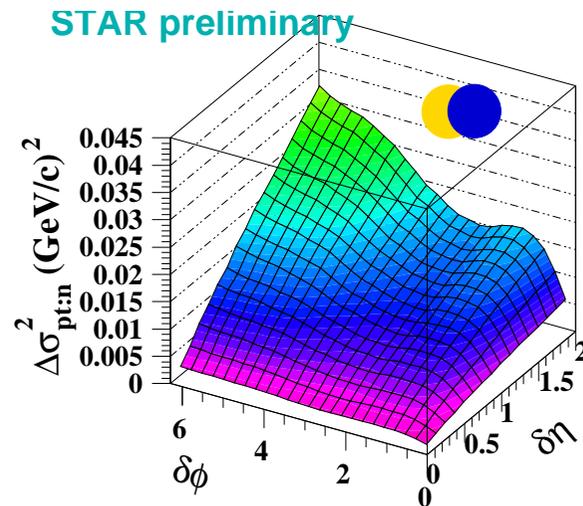
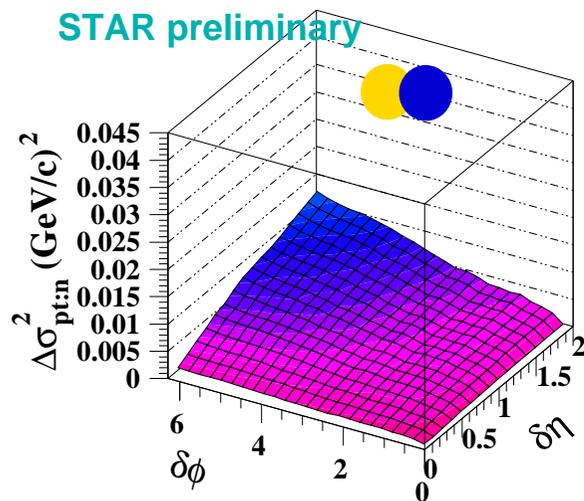
reference density ρ_{ref} makes a per-particle measure:

$$\rho_{\text{ref}} \propto \bar{n}^2 \Rightarrow \frac{1}{\sqrt{\rho_{\text{ref}}}} \propto \frac{1}{\bar{n}} \quad (13)$$

$$\Delta\sigma_{p_t:n}^2(m_\delta \varepsilon_\eta, n_\delta \varepsilon_\phi) = 4 \sum_{k,l=1}^{m_\delta, n_\delta} \varepsilon_\eta \varepsilon_\phi K_{m_\delta n_\delta:kl} \frac{\Delta\rho(p_t : n; k\varepsilon_\eta, l\varepsilon_\phi)}{\sqrt{\rho_{\text{ref}}(n; k\varepsilon_\eta, l\varepsilon_\phi)}} \quad (14)$$

Inverse problem: knowing $\Delta\sigma^2$, solve for $\Delta\rho/\sqrt{\rho_{\text{ref}}} \Rightarrow$ save $O(N)$ in CPU time !

19 p_t correlations from the inversion

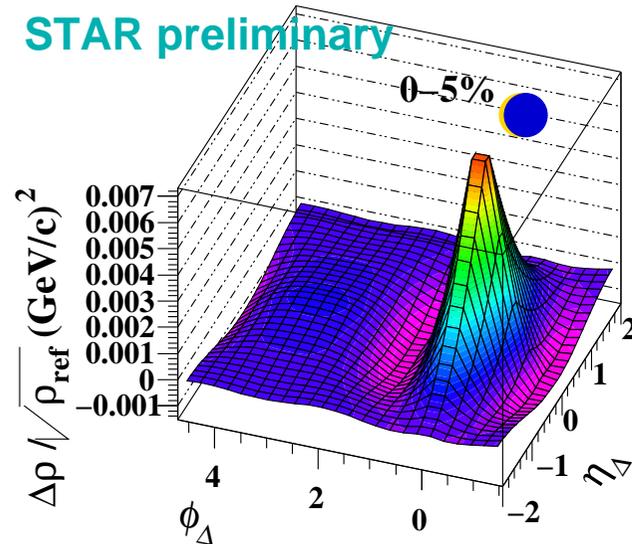
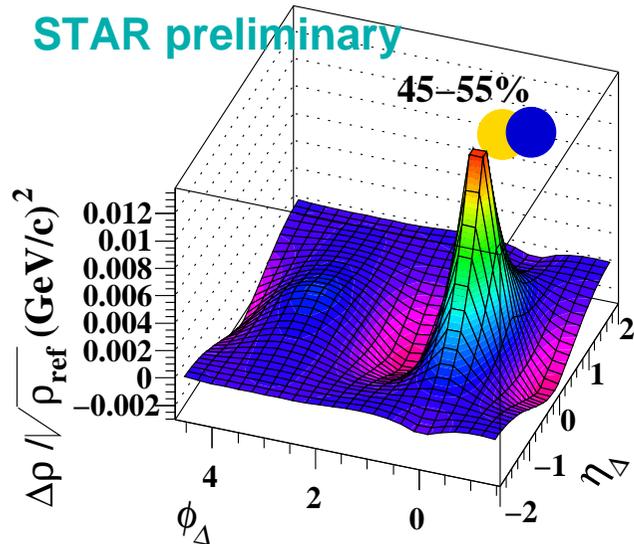
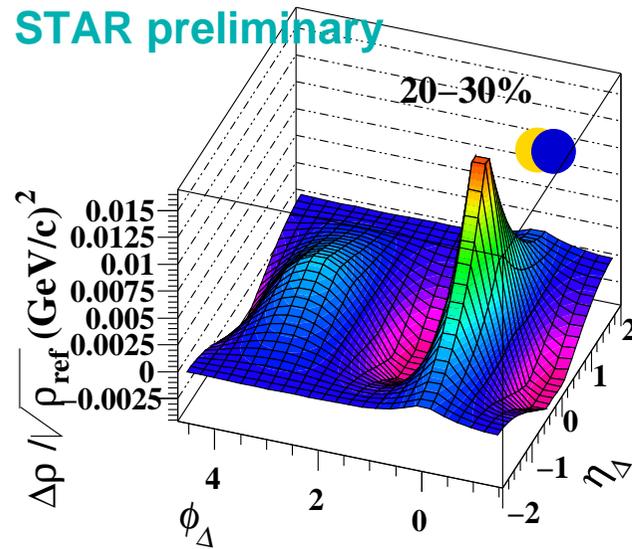
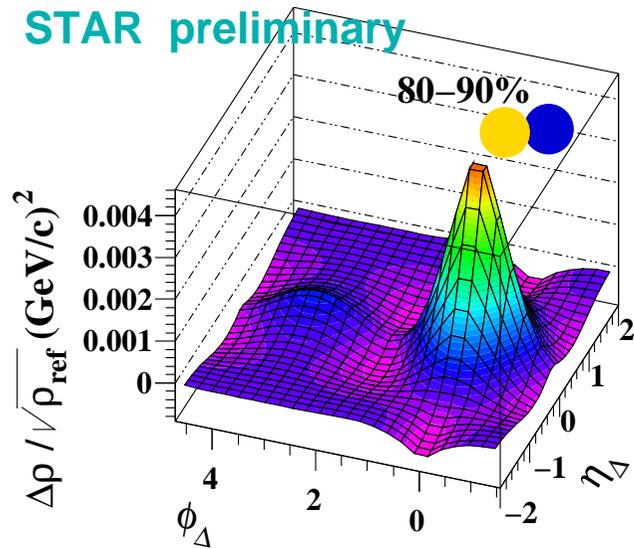


Top:
scale dependence of
the “pure” p_t variance.

Bottom:
corresponding
autocorrelation

First direct evidence of elliptic flow as a p_t blast.
Next, subtract the flow contribution to look at
minijets.

20 Localized p_t correlations: minijets



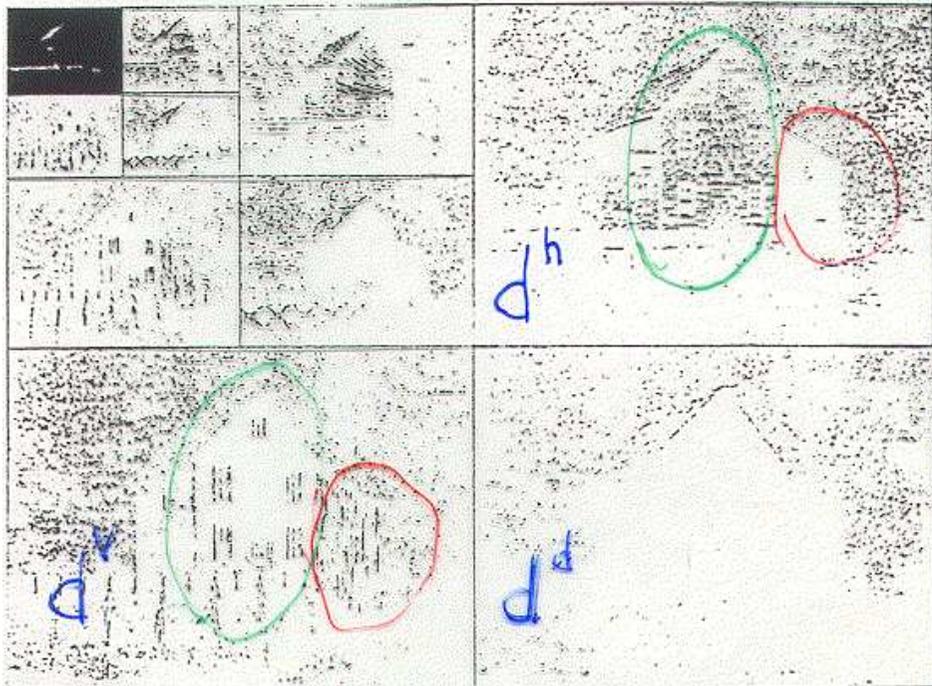
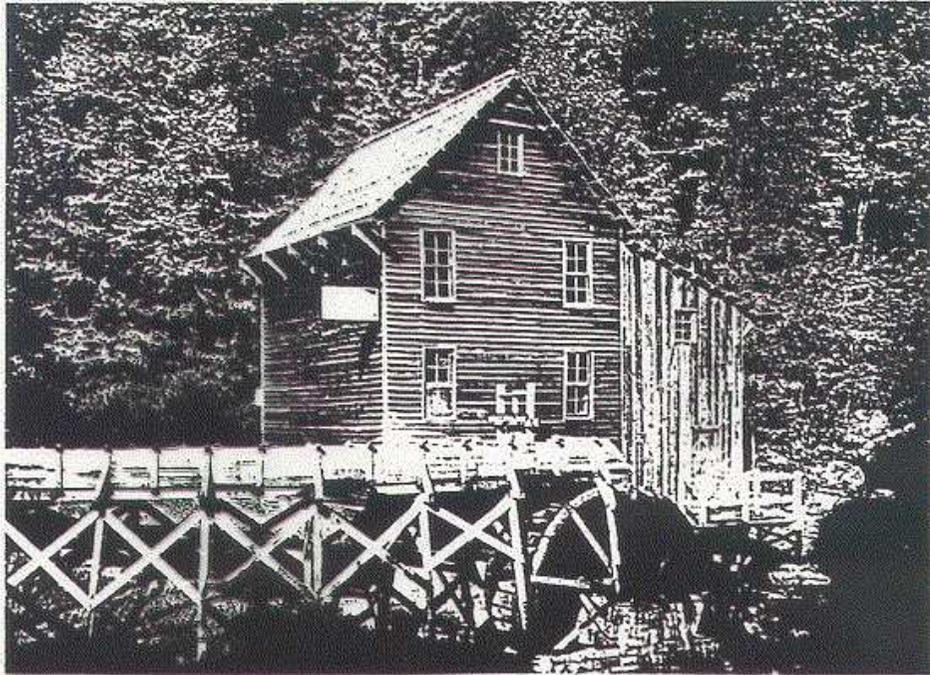
AuAu 200 GeV. In η , correlation broadens with centrality; in ϕ the trend is opposite. The surrounding background seems to recoil.

21 Conclusions

- Semi-hard scattering leaves a trace in the soft p_t domain – new at RHIC !
- First direct measurements of p_t correlation structure reveal azimuthal anisotropy of p_t field \Rightarrow elliptic flow is a velocity phenomenon
- The minijet correlation structure is modified with centrality; the effect appears to “turn on” around $\nu = (N_{\text{part}}/2)^{1/3} \approx 3$. Broadening of the correlation in η and weakening of P_{dyn}^η on the coarse scale are consistent descriptions of the effect. How exactly does the coupling between longitudinal flow and mini-jets work ? What do we learn about the expanding fluid ?
- Increased symmetry of the charge-dependent correlation on (η, ϕ) in the central collisions may point to a change in the hadronization geometry in the medium

22 Extra slides

23 DWT of a photographic image



Reproduced from textbook:
I. Daubechies, "Ten lectures on wavelets". The original caption: "A real image, and its wavelet decomposition into three multiresolution layers. On the wavelet components one clearly sees that the $d^{j,v}$, $d^{j,h}$, $d^{j,d}$ emphasize, respectively, vertical, horizontal, and diagonal edges. In this figure, the bottom picture has been overexposed to make details in the $d^{j,\lambda}$ more apparent. I would like to thank M. Barlaud for providing this figure." The colored marks are mine.